

1                   **DEVELOPING CHEMICAL ENGINEERING ACUMEN,**  
2                                   **by Brewing *Kicking Mule Beer***

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14 The Kicking Mule Brewing Co. at West Point enables members of our chemical engineering club,  
15 students, and beer enthusiasts alike to acquire chemical engineering acumen, knowledge, and skills  
16 by developing a tangible product. Through a rigorous on-site brewing process with subject matter  
17 experts, our goal is enhancement of student chemical engineering knowledge with respect to batch  
18 reactors and mixtures, heat exchange processes, process control, and bio-chemical reaction  
19 kinetics while simultaneously providing quality products to The United States Corps of Cadets.

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22 **INTRODUCTION**

23  
24           Batch quantity beer production at West Point serves a number of audiences: the  
25 American Institute of Chemical Engineering (AIChE) Student Chapter, cadets and faculty, and  
26 the chemical engineering curriculum. This is optional for Chemical Engineering cadets and is  
27 open to any interested cadet. Beer making is a nearly ideal process to demonstrate a wide variety  
28 of chemical engineering concepts and has recently served this purpose at several other  
29 undergraduate institutions.<sup>[1, 2, 3, 4, 5, 6]</sup> Heat transfer, reactor design and kinetics, process control,  
30 separations, and basic unit operations are all included in one process, and the data analysis has  
31 the potential to tie into our Chemical Engineering electives in our eight semester academic  
32 sequence.<sup>[7, 8, 9, 10, 11]</sup> We will articulate this potential in the Discussion section.

33           The process begins with the creation of wort, which is the sugary precursor to beer. Wort  
34 contains the sugars necessary for fermentation in addition to hops for flavor, bitterness, and  
35 aroma. In our process, cadets create the wort from milled grain by cooking the grain in an

1 aqueous batch reactor (also known as the “mash tun” in the vernacular of beer brewing). The  
2 heat of cooking activates enzymes that break down long-chain sugars into short-chain,  
3 fermentable, sugars. This process exposes cadets to concepts taught in Separation Processes  
4 classes, such as solid-liquid extraction and leeching.<sup>[6, 11]</sup>

5         When yeast is added following the production of the wort (the mash with the grain solids  
6 removed), cadets also get an introduction to the overlap of chemical and bioengineering.  
7 Because the yeast cells are alive, undergoing their lifecycle from cell birth to cell growth and cell  
8 apoptosis, this batch system, in addition to brewing the beer, is also a bioreactor. The sugar and  
9 temperature must be controlled under a range that would optimize the yeast life cycle and  
10 produce ethanol.<sup>[5,6]</sup> Maintaining and engineering adequate conditions for the life cycle of the  
11 yeast cells has clear ties to biological engineering.

12         Temperature control is important throughout the beer brewing process. During wort  
13 production, the temperature at which the enzymes are activated will produce longer- or shorter-  
14 chain sugars leading to more- or less-fermentable sugars. By controlling the temperature  
15 throughout the fermentation process, students have the opportunity to collect kinetic reaction  
16 data. They collect this data using a refractometer, hydrometer, and gas chromatograph with mass  
17 spectrometric detection (GC-MS). After collecting data from several fermentations (at least  
18 three), they can model the data using the Parallel Tempering Algorithm, which is a recently  
19 published global, stochastic data fitting optimization algorithm with several appropriate bio-  
20 kinetic models used for the production of ethanol.<sup>[6,12,13]</sup> While accounting for the variables of  
21 sugar consumption rates, ethanol production rates, and biomass content, cadets fit their  
22 experimental data to models from literature, which includes the Monod, Aiba, Tiessier and  
23 Hinshelwood models<sup>[13-17]</sup>. By modeling the data, students observe how the temperature of the

1 fermenter affects the reaction rate. A higher fermenter temperature yields a faster, more vigorous  
2 fermentation reaction rate.

3 Our beer brewing process uses a countercurrent plate heat exchanger to chill the wort from  
4 boiling to a temperature suitable for fermentation in a single pass of tap water. By adjusting the  
5 wort flow rates with a pump, and the countercurrent cold water with a faucet, students can achieve  
6 the optimal flow rates and temperatures to chill the wort for fermentation. Cadets use this  
7 information to calculate the heat transfer parameters for the heat exchanger. After seeing the  
8 application of the heat exchanger, cadets model the process in CHEMCAD using a countercurrent  
9 heat exchanger unit to develop their capabilities with the software and to gain confidence in  
10 performing an energy balance on a practical, working, system.<sup>[8, 10]</sup>

11 The remainder of the paper is as follows: we will demonstrate how the Kicking Mule  
12 Beer brewing process incorporates chemical engineering aspects and facilitates development of  
13 acumen in chemical reaction engineering, data fitting and optimization, lab data analysis, and  
14 process controls. We first show the collected reactant and product vs. time data for three batches  
15 of Kicking Mule beer and fit the data to published bio-kinetic models. We fit the model  
16 parameters to the data using a recently published optimization algorithm. We then show how we  
17 calculate the overall heat transfer coefficients for all of our heating and cooling equipment using  
18 best practices outlined in literature. Following this effort, we record transient temperature control  
19 information on our PID temperature controlling device. Finally, with our modeling and  
20 parametric analysis complete, we use the CHEMCAD software to model parts of the process.  
21 Each of these subtopics is a course, or a part of one of our courses, readers can see a list of all  
22 required courses at <https://www.usma.edu/chemistry/SitePages/Chemical%20Engineering.aspx>.

23

## 1   **APPARATUS AND METHODS**

2           The beer brewing system used by cadets in our program is a professional, three-vessel,  
3 electric system used to brew beer from grain. This system gives industry-level precision for  
4 temperatures and controls. The system is an Electric Heat Exchange Recirculating Mash System  
5 (E-HERMS) and allows for multiple levels of control throughout the brewing process from the  
6 mash to the boil and then to the fermenter which is also temperature controlled, and therefore the  
7 control aspect of this process can also be modeling in the context of our Chemical Engineering  
8 Process Controls course.<sup>[9]</sup>

9           The beginning of the brewing process starts with recipe selection, to include types and  
10 roasts of grains, types and amounts of hops, and strain of yeast for fermentation. Once the recipe  
11 is finalized, the grain is milled to expose the starches and subsequently maximize the contact  
12 time of the starches with the water. The process of cooking the starches out of the grain to  
13 produce the “mash” occurs in the far-left vessel of the E-HERMS shown in Figure 2a.

14           To activate the desired enzymes when the milled grain is mixed with heated water, the  
15 temperature must be precisely regulated. The mash needs to be held at a constant temperature  
16 for about an hour and our system uses a constant recirculation of the mash through a coiled heat  
17 exchanger which is immersed in a water bath in the middle tank, called the hot liquor tank  
18 (HLT). The constant recirculation is achieved through a gravity primed liquid pump and high  
19 temperature hoses. The water in the hot liquor tank is heated and the temperature regulated  
20 through a Proportional-Integral-Derivative (PID) controller and an electric heating element. The  
21 main control panel allows for exact PID control of the temperature in the HLT which in turn  
22 transfers heat to the mash through the heat exchanger. This allows for indirect heating of the  
23 mash during starch conversion which mitigates any scorched grains and off flavors from direct

1 fired heating. The constant recirculation also allows for the water in the mash to be drawn  
2 through the grain bed, which settles, and acts as a filter giving a clearer product. This portion of  
3 the process allows for hands-on application of controls as well as unit operations.

4         Once the mash has finished its conversion, which is monitored with a refractometer to  
5 ensure completion, the fully converted sugar solution, called wort, is pumped to the far-right  
6 vessel, shown in Figure 2a, the boil kettle. This demonstrates real world plant-type operations in  
7 determining which valves need to be closed, which hoses need to be moved, and which pumps  
8 need to be running.

9         When the wort is completely transferred, it is boiled. The boil kettle also uses an electric  
10 heating element to provide energy. The element uses a separate controller to regulate output from  
11 0-100% power. This gives cadets another step to control and minimize energy use while still  
12 maintaining a rolling boil. During the boil, hops are added. By regulating the amount, variety,  
13 and time at which the hops are added during the boil, cadets can affect the characteristics of the  
14 final product. Specifically, by varying the boil time, the alpha acids in the hops contribute to a  
15 spectrum of characteristics, including aroma, flavor, and bitterness. At the conclusion of the boil,  
16 the wort needs to be cooled rapidly in order to reach a temperature conducive to yeast  
17 fermentation.

18         Post-boil processing is critical for the wort, as the transition from the boil kettle to the  
19 sanitized fermenter exposes the product to potential infection from airborne bacteria or wild  
20 yeast. Cooling rapidly with minimum contact time to the atmosphere reduces the chance for  
21 contamination as well as minimizing process time. In order to accomplish this, we use a counter-  
22 current plate heat exchanger shown in Figure 2c. The wort is sent through the sanitized heat  
23 exchanger, with regular tap water run counter-currently. By regulating the flow rates of both the

1 wort and the tap water cadets can achieve the desired temperature, usually about 68 °F,  
2 maximize flow rate of the wort, and minimize exposure to bacteria. After the wort is cooled, it is  
3 moved to the unagitated fermenter shown in Figure 2b. The fermenter is equipped with both a  
4 heating pad and Peltier coolers in order to regulate the temperature during fermentation. The  
5 fermenter also has a side valve to take samples during fermentation. The cadets track  
6 fermentation using multiple analytical methods.

7         Three main methods are used to track ethanol production, as well as sugar consumption,  
8 over time. The first method employs an industry standard hydrometer. The density of the wort  
9 changes as sugar is converted to ethanol, changing the level the hydrometer floats. We also used  
10 a refractometer which uses the refractive index of the wort solution to track sugar content. This  
11 method is not as widely used, as the addition of ethanol, as well as biomass, in the solution,  
12 skews the refraction. While it is possible to compensate, the refraction method is not as accurate  
13 for active fermentation and, because of the large uncertainty associated with it, we did not  
14 include this data in our analysis.

15         The final method we use is GC-MS, specifically, a polar Supelcowax capillary column  
16 (30m x 0.2mm x 0.2 $\mu$ m). We used the internal standard calibration method with methanol as the  
17 internal standard. We used an oven temperature program of: 1 min at 40°C, ramp to 240°C at  
18 100°C per min, and then holding at 240°C for 30 seconds. Samples were filtered using 0.2 $\mu$ m  
19 filters before adding the internal standard. This allows a very precise measurement of alcohol  
20 production over time, incorporating our chemistry majors by bringing a new and practical project  
21 into their laboratory experience. These methods are then compared to see if they correlate, while  
22 also providing multiple data sets to use for kinetic modeling. An example of the consistency and  
23 corroboration of the hydrometer reading and GC-MS is shown in the results section.

a.



b.



1

c.



2 **Figure 2.** Brewing apparatus: a. E-HERMS.; b. Fermentation reactor; c. Blichmann Heat  
3 Exchanger

4

### 5 **SAFETY**

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The brewing process pedagogical method provides the perfect opportunity to discuss

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process safety and demonstrate the need to imbed safety in the design process. Safety concerns

9

include burning hazards, electrical hazards, and the typical “slips, trips and falls” risk that is

10

ubiquitous in all chemical engineering plant operations. Cadet leadership was directed to ensure

1 safety best practices were followed. A formal written risk assessment is briefed prior to  
2 operations and safety measures are enforced throughout the process, as per the Cadets Safety and  
3 Chemical Engineering Education (SACHE) training, that all of the senior Cadets must take in  
4 conjunction with their Senior Chemical Engineering Lab Course.

## 5 **DATA ANALYSIS**

### 6 **Yeast Fermentation Kinetics Analysis**

7         Brewing beer is a bioprocess in which the consumption of sugar by living yeast cells  
8 produces two products: the desired product, ethanol, and undesired biomass. From a reaction  
9 kinetics perspective, this is not a convenient first-, second-, or even fractional-order reaction with  
10 which our students are generally familiar. Determining an appropriate model (rate law) which  
11 they can then apply to their knowledge of reactor design is a critical skill. This methodology  
12 also provides background for discussions about whether achieving models that follow from first  
13 principles is necessary or desired, or if the data takes precedent when designing or scaling  
14 systems.

15         For the kinetic reaction data presented in this paper, three modeling equations were used.  
16 The model representing the production of biomass given by Eq. 1 below, where all  
17 concentrations are mass-based:

$$18 \quad \text{Biomass: } \frac{dX}{dt} = \mu(t)X(t) \quad , \quad (1)$$

19 where  $X$  is the concentration of cells and  $\mu(t)$  is the specific growth or kinetic reaction rate with  
20 respect to time. The production of the desired product, ethanol, follows a similar model given by  
21 Eq. 2:



1

$$\text{Ethanol: } \frac{dP}{dt} = q(t)X(t), \quad (2)$$

2 where  $P$  is the ethanol concentration, and  $q(t)$  is the product accumulation rate. The ethanol  
3 production model shows a rate of increase of product concentration  $P$  with respect to time given  
4 cell concentration  $X$  and kinetic rate of reaction  $q(t)$ . These models are reliant on the  
5 consumption of the substrate sugar. The rate of consumption of sugar is given by equation Eq. 3:

6

$$\text{Sugar: } \frac{dS}{dt} = -\frac{1}{Y_{x/s}} \frac{dX}{dt} - \frac{1}{Y_{p/s}} \frac{dP}{dt}, \quad (3)$$

7 where  $S$  is the concentration of the sugar, and  $Y_{x/s}$  and  $Y_{p/s}$  are the yield coefficients<sup>[13-17]</sup>. The  
8 rate of consumption of substrate  $S$  is in proportion with the rates of production of both the cell  
9 concentration  $X$  and the product concentration  $P$ . The ratio of both products produced from the  
10 consumed substrate are represented by the yield coefficients  $Y_{x/s}$  and  $Y_{p/s}$ .<sup>[13-17]</sup>

11 The following models from literature depict the fermentation process over time. In each  
12 model,  $\mu(t)$  represents the specific growth rate and  $q(t)$  represents the specific product  
13 accumulation rate. The function  $S(t)$  is the concentration of substrate over time and is a term in  
14 each of the four kinetic models we model with the ethanol data presented here. The Aiba and  
15 Hinshelwood models include the function  $P(t)$  representing the concentration of the product  
16 ethanol over time.<sup>[13-17]</sup> As shown in Eqs. 4-7, each of the four models have unique expressions  
17 for the specific growth rate  $\mu(t)$  and the specific product accumulation rate  $q(t)$ . Table 1 has a  
18 listing and description of each of the respective model parameters.

19

1 **MONOD:**

2

$$\begin{aligned}\mu &= \mu_{\max} \left( \frac{S(t)}{K_{sx} + S(t)} \right) \\ q &= q_{\max} \left( \frac{S(t)}{K_{sp} + S(t)} \right)\end{aligned}\tag{4}$$

3 **TESSIER:**

4

$$\begin{aligned}\mu &= \mu_{\max} \left( 1 - \exp \left\{ -\frac{S(t)}{K_{sx}} \right\} \right) \\ q &= q_{\max} \left( 1 - \exp \left\{ -\frac{S(t)}{K_{sp}} \right\} \right)\end{aligned}\tag{5}$$

5 **AIBA:**

6

$$\begin{aligned}\mu &= \mu_{\max} \left( \frac{S(t)}{K_{sx} + S(t)} \right) \exp \{ -K_{ix} P(t) \} \\ q &= q_{\max} \left( \frac{S(t)}{K_{sp} + S(t)} \right) \exp \{ -K_{ip} P(t) \}\end{aligned}\tag{6}$$

7 **HINSHELWOOD:**

8

$$\begin{aligned}\mu &= \mu_{\max} \left( \frac{S(t)}{K_{sx} + S(t)} \right) (1 - K_{ix} P(t)) \\ q &= q_{\max} \left( \frac{S(t)}{K_{sp} + S(t)} \right) (1 - K_{ip} P(t))\end{aligned}\tag{7}$$

9

<b>Model</b>	<b>Parameter</b>	<b>Units</b>	<b>Description</b>
<b>Monod &amp; Tessier</b>	$\mu_{\max}$	$d^{-1}$	model parameter
	$K_{sx}$	$g\ dm^{-3}$	model parameter
	$q_{\max}$	$g\ (g\ d)^{-1}$	model parameter
	$K_{sp}$	$g\ dm^{-3}$	model parameter
	$Y_{x/s}$	-	yield coefficient
	$Y_{p/s}$	-	yield coefficient
<b>Aiba &amp; Hinshelwood</b>	$\mu_{\max}$	$d^{-1}$	model parameter
	$K_{sx}$	$g\ dm^{-3}$	model parameter
	$q_{\max}$	$g\ (g\ d)^{-1}$	model parameter
	$K_{sp}$	$g\ dm^{-3}$	model parameter
	$Y_{x/s}$	-	yield coefficient
	$Y_{p/s}$	-	yield coefficient
	$K_{ix}$	$g\ dm^{-3}$	model parameter
	$K_{ip}$	$g\ dm^{-3}$	model parameter

### MODEL FITTING PROCEDURE

The data is collected for each of the three runs via a hydrometer and the current density is correlated with a sugar and ethanol concentration. At the beginning of the reaction there is a lag of approximately 24-36 hours and then a quick ramp up in ethanol production and sugar consumption. Therefore, we frontload a greater frequency of data collection for the first 3-4 days of the reaction, with 3-4 readings per 24-hour period. We record data for approximately 8-10 days, taking 2 – 3 readings per 24-hour period.

However, empirical data for the biomass cell count needed for the models could not be collected and so there was no yeast concentration vs time data to incorporate into the ODEs. With the data we did collect, we executed a stochastic minimization, parallel tempering-like, algorithm<sup>[12]</sup> for each of the data sets of sugar and ethanol and allowed the stochastic models to

1 find the “best fit parameters” for each of the kinetic models, including the kinetic parameter for  
2 yeast. Each of the kinetic models was fit with the stochastic algorithm a total of five times with  
3 randomized initial guess, and the parameter values yielding the smallest  $F_{\text{cost}}$  were recorded, as  
4 well as the average and standard deviation from each of the 5 fits for each of the models, for each  
5 of the three data sets. Because the minimization algorithm is stochastic and global, there is a  
6 different value for each of the “best-fit” parameter values on each of the runs, with a different  
7 value of cost function, shown in Eq. 8. In addition, we calculate a residual sum of squares (RSS)  
8 value for each run, shown in Eq. 9.<sup>[12]</sup> Lastly we incorporate an Akaike Information Criteria  
9 (AIC), shown in Eq. 10, for each best model fit, which attempts to “level the playing field by  
10 assigning a penalty for over-fitting data sets, whereby models with more parameters are  
11 penalized more than lower parameter counterparts<sup>[18]</sup>.

12 For the parallel tempering algorithm, we run  $N_{\text{run}}$  number of separate, yet parallel runs,  
13 whereby new parameters are guesses based on a search algorithm. Each of the runs is at a different  
14 “Boltzman Energy” ( $E_B$ ), in such a way that there is a larger parameter space explored the higher  
15 the  $E_B$ , and higher probability of keeping a set of parameters that produce a larger value of  $F_{\text{cost}}$ .  
16 Lastly, the algorithm pauses at prearranged times to compare parameter values with neighbor runs  
17 to the left and right. Parameter sets yielding values of are slowly shifted to the “cold” side over  
18 time, thereby producing the best fit set of parameters. We run each fit for each data set and each  
19 respective model five times. We chose to run each model for each data set five times to give us a  
20 large enough population of fit model parameters to enable the calculation of average and standard  
21 deviation for each parameter fit. By using a stochastic fitting algorithm, gathering and reporting  
22 statistics allows a deeper understanding of the kinetic models and the dynamic process, and also  
23 allows reporting each parameter average and standard deviation shown in Table 2a-c.<sup>[12-17]</sup>

1            There a  $N_{run}$  number of “Energy Levels”, whereby new parameters are guessed; if the new  
 2 set of parameters produce a better cost function value they are kept; while there is a probability  
 3 ( $P_A$ ) of acceptance even when there is no improvement based on cost function value. Over the  
 4 course of the algorithm running, “nearest neighbor” energy levels compare parameter and cost  
 5 function values, and exchange parameters sending the best parameter values based on cost function  
 6 to the colder end of the flow chart. The cost function is computed as follows<sup>[12]</sup>:

$$7 \quad F_{cost} = \sum_i^N \left( \sqrt{(f_{EtOH,i} - y_{EtOH,i})^2 + (f_{GLUC,i} - y_{GLUC,i})^2} \right) / 2 \quad , \quad (8)$$

8 where  $f_i$  is the model prediction of concentration and  $y_i$  is the actual concentration. The residual  
 9 sum of squares is shown below, and is another useful metric required for the AIC calculation:

$$10 \quad \text{Mod. RSS} = \sum_i^N \left( \sqrt{(f_{EtOH,i} - y_{EtOH,i})^2 + (f_{GLUC,i} - y_{GLUC,i})^2} \right) / 2N \quad . \quad (9)$$

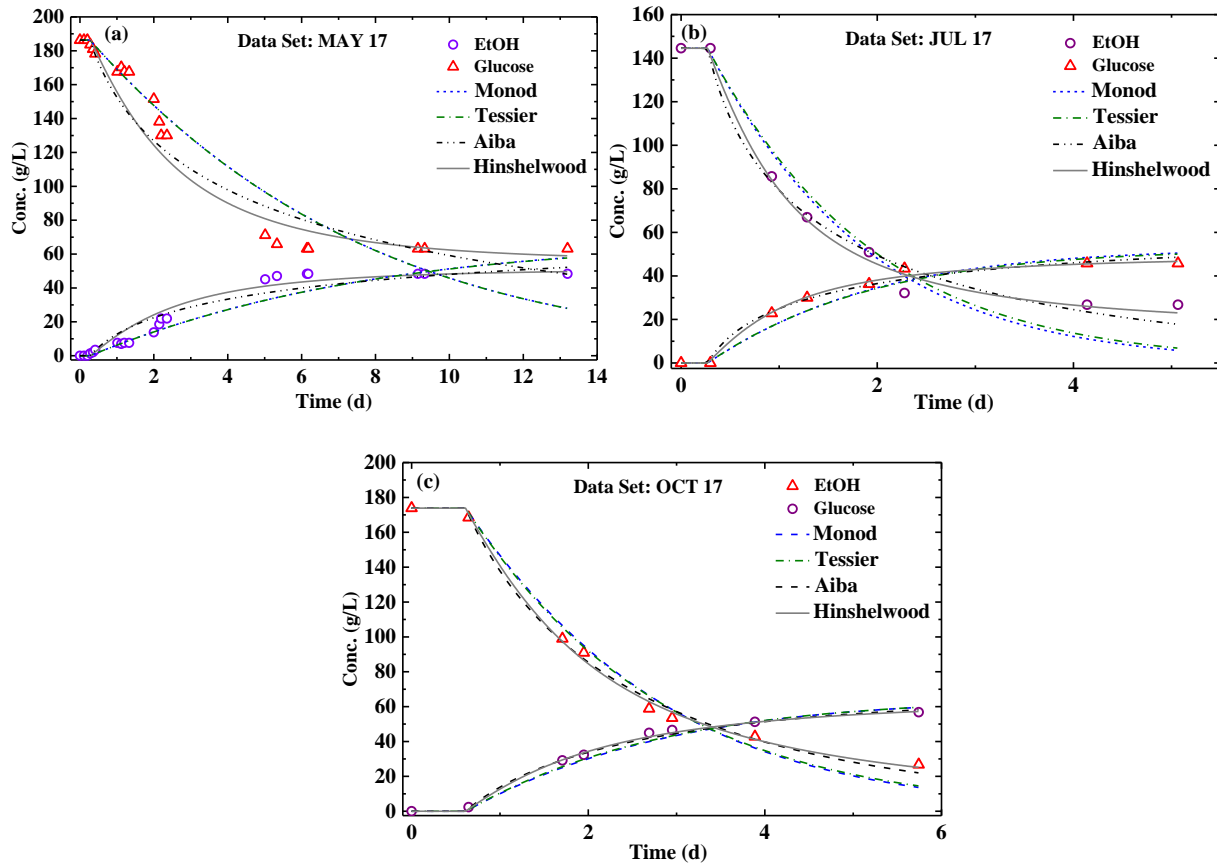
11  
 12 Lastly the AIC is calculated per equation 10,  
 13

$$14 \quad \text{AIC} = 2k + 2 \ln(\text{Mod. RSS}) \quad , \quad (10)$$

15  
 16 where  $k$  is the number of model parameters, and RSS is the residual sum of squares<sup>[12]</sup>  
 17

## 18 19 20 **MODEL FITTING RESULTS**

21  
 22            The four model fitting results are shown below in Figure 4a-c. The additional two  
 23 parameters utilized by the Aiba and Hinshelwood models give slightly better fits for modeling  
 24 the ethanol production and glucose consumption vs time, as demonstrated by the lower cost  
 25 functions.  
 26



**Figure 4a** Ethanol and glucose vs. time kinetic data of the Kicking Mule Brewery run from May 2017; **b** July 2017; **c** October 2017. Depicted are the model fits using the Monod, Tessier, Aiba, and Hinshelwood kinetic models.

The values of the best fit parameters for the Monod, Tessier, Aiba, and Hinshelwood models, for each of the data sets along with averages,  $\mu$ , and standard deviations,  $\sigma$ , are shown in Table 2a-d below.<sup>[13-17]</sup>

Parameter	May-17			Jul-17			Oct-17			units
	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	
$\mu_{max}$	<b>0.30</b>	0.32	0.03	<b>0.66</b>	0.27	0.12	<b>0.446</b>	0.426	0.012	$d^{-1}$
$K_{sx}$	<b>3720</b>	2200	990	<b>9200</b>	9100	400	<b>8710</b>	9390	650	$g\ dm^{-3}$
$K_{sp}$	<b>640</b>	320	280	<b>545</b>	533	53	<b>675</b>	634	34	$g\ (g\ d)^{-1}$
$q_{pmax}$	<b>1090</b>	610	410	<b>4200</b>	4200	320	<b>4070</b>	3860	180	$g\ dm^{-3}$
$Y_{x/s}$	<b>0.88</b>	0.44	0.56	<b>5.3E-06</b>	0.013	0.027	<b>0.61</b>	0.80	0.22	-
$Y_{p/s}$	<b>0.4</b>	4.2	3.1	<b>0.66</b>	0.54	0.11	<b>0.372</b>	0.373	0.001	-

**Table 2b**  
Best fit Tessier model parameters for May 2017, July 2017, and October 2017; w/ ave. and stdev.

Parameter	May-17			Jul-17			Oct-17			units
	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	
$\mu_{\max}$	<b>0.31</b>	0.32	0.01	<b>0.37</b>	0.43	0.02	<b>0.43</b>	0.42	0.02	$d^{-1}$
$K_{sx}$	<b>3300</b>	3000	1100	<b>9950</b>	9840	180	<b>8860</b>	9160	530	$g\ dm^{-3}$
$K_{sp}$	<b>530</b>	460	220	<b>628</b>	595	25	<b>653</b>	630	19	$g\ (g\ d)^{-1}$
$q_{pmax}$	<b>840</b>	760	340	<b>4560</b>	4310	180	<b>3720</b>	3600	110	$g\ dm^{-3}$
$Y_{x/s}$	<b>1.21</b>	0.90	0.79	<b>0.52</b>	0.47	0.34	<b>0.62</b>	0.70	0.28	-
$Y_{p/s}$	<b>0.37</b>	0.72	0.46	<b>0.3650</b>	0.3638	0.0007	<b>0.3740</b>	0.3748	0.0007	-

**Table 2c**  
Best fit Aiba model parameters for May 2017, July 2017, and October 2017; w/ ave. and stdev.

Parameter	May-17			Jul-17			Oct-17			units
	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	
$\mu_{\max}$	<b>0.15</b>	0.15	0.01	<b>0.43</b>	0.14	0.04	<b>0.39</b>	0.41	0.01	$d^{-1}$
$K_{sx}$	<b>9750</b>	9740	470	<b>9450</b>	9890	870	<b>9130</b>	9170	300	$g\ dm^{-3}$
$K_{sp}$	<b>850</b>	1040	120	<b>131.4</b>	1.9	5.5	<b>317</b>	304	28	$g\ (g\ d)^{-1}$
$q_{pmax}$	<b>3950</b>	4000	110	<b>3730</b>	4880	470	<b>3700</b>	3480	140	$g\ dm^{-3}$
$Y_{x/s}$	<b>0.053</b>	0.031	0.016	<b>0.03</b>	0.34	0.47	<b>1.2</b>	1.5	0.4	-
$Y_{p/s}$	<b>0.378</b>	0.374	0.005	<b>0.38</b>	0.28	0.05	<b>0.384</b>	0.382	0.002	-
$K_{ix}$	<b>15.1</b>	14.6	4.3	<b>20.2</b>	1.4	1.3	<b>12.5</b>	7.3	2.8	$g\ dm^{-3}$
$K_{ip}$	<b>0.035</b>	0.030	0.003	<b>0.039</b>	0.022	0.007	<b>0.019</b>	0.017	0.002	$g\ dm^{-3}$

**Table 2d**  
Best fit Hinshelwood model parameters for May 2017, July 2017, and October 2017; w/ ave. and stdev.

Parameter	May-17			Jul-17			Oct-17			units
	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	Best	$\mu$	$\sigma$	
$\mu_{\max}$	<b>0.18</b>	0.16	0.02	<b>0.42</b>	0.41	0.01	<b>0.40</b>	0.42	0.01	$d^{-1}$
$K_{sx}$	<b>10860</b>	10290	920	<b>8848</b>	8932	95	<b>9340</b>	9940	920	$g\ dm^{-3}$
$K_{sp}$	<b>1040</b>	1134	52	<b>200</b>	209	5	<b>381</b>	395	12	$g\ (g\ d)^{-1}$
$q_{pmax}$	<b>3710</b>	3960	140	<b>3350</b>	3460	60	<b>3420</b>	3539	79	$g\ dm^{-3}$
$Y_{x/s}$	<b>0.13</b>	0.15	0.10	<b>0.95</b>	0.74	0.32	<b>0.92</b>	1.04	0.27	-
$Y_{p/s}$	<b>0.390</b>	0.389	0.001	<b>0.38</b>	0.37	0.02	<b>0.384</b>	0.384	0.001	-
$K_{ix}$	<b>5.0</b>	5.5	0.4	<b>7.5</b>	7.7	0.3	<b>2.0</b>	2.4	0.3	$g\ dm^{-3}$
$K_{ip}$	<b>7.9E-07</b>	2.1E-05	1.9E-05	<b>3.1E-06</b>	2.7E-06	1.1E-06	<b>0.0022</b>	0.0005	0.0009	$g\ dm^{-3}$

The overall model comparisons for each data set are shown in Tables 3a-c for each of the respective ethanol and glucose data sets from May 2017, July 2017 and October 2017. In this case, having more parameters improves the modeling of the sugar and ethanol concentrations,

1 per the decreased cost function numbers. This, however, comes with a penalty as shown by the  
 2 respective increased AIC values. This is a critical lesson on modeling and optimization for the  
 3 cadets. In this case, the addition of two model parameters is potentially justified because of the  
 4 better fit (cost function); however, this will not necessarily be true for all models. As seen in  
 5 Tables 3a-c, the parameter penalty does not significantly change the comparison.<sup>[13-17]</sup> The best  
 6 models are then carried forward for use in our Chemical Reactor Design course, CH364 in  
 7 Figure 1, to model batch reactors. With the kinetic models above, and best fit parameters, one  
 8 can modify the kinetic equations in CHEMCAD with excel Macros and model the batch reactor,  
 9 obtaining the correct reactor volume that will agree with the actual fermentation reactor volume.

<b>Table 3a</b>					
<b>May 2017 Data, Model Comparison</b>					
<b>Model</b>	<b>No. Parameters</b>	<b>N</b>	<b>Cost Function</b>	<b>Modified RSS</b>	<b>AIC</b>
<b>Monod</b>	6	1320	383	0.30	9.5
<b>Tessier</b>	6	1320	376	0.28	9.5
<b>Aiba</b>	8	1320	275	0.21	12.9
<b>Hinshelwood</b>	8	1320	196	0.15	12.2

<b>Table 3b</b>					
<b>July 2017 Data, Model Comparison</b>					
<b>Model</b>	<b>No. Parameters</b>	<b>N</b>	<b>Cost Function</b>	<b>Modified RSS</b>	<b>AIC</b>
<b>Monod</b>	6	507	130	0.26	9.3
<b>Tessier</b>	6	507	127	0.25	9.2
<b>Aiba</b>	8	507	63	0.12	11.8
<b>Hinshelwood</b>	8	507	30	0.059	10.3

<b>Table 3c</b>					
<b>October 2017 Data Model Comparison</b>					
<b>Model</b>	<b>No. Parameters</b>	<b>N</b>	<b>Cost Function</b>	<b>Modified RSS</b>	<b>AIC</b>
<b>Monod</b>	6	575	92	0.16	8.3
<b>Tessier</b>	6	575	84	0.15	8.2
<b>Aiba</b>	8	575	41	0.071	10.7
<b>Hinshelwood</b>	8	575	31	0.054	10.2



1  
2

3 To validate our data collection activities using the hydrometer, which was the basis of the kinetic  
4 model fitting optimization, we compare the GC-MS and hydrometer data for the ethanol  
5 concentration in Table 4. As seen, the two methods agree to within 10%.

No.	Date	Time (hrs)	Running Time (min)	Hydrometer specific gravity	Hydrometer ABV(%)*	glucose conc. (mol/L)	GC-MS ABV(%)
1	2-Oct	1612	0		0	-	-
2	3-Oct	740	928	1.063	0.3	0.93618	0.3±0.2
3	4-Oct	910	2458	1.037	3.7	0.54982	3.6±0.2
4		1500	2808	1.034	4.1	0.50524	3.8±0.2
5	5-Oct	845	3873	1.022	5.7	0.32692	5.3±0.2
6		1500	4248	1.02	5.9	0.2972	-
7	6-Oct	1330	5598	1.016	6.5	0.23776	7.0±0.2
8	8-Oct	1000	8268	1.010	7.2	0.1486	-

6 \* The ABV value was calculated from the specific gravity using a Brix scale. Calculators for  
7 brewers can be found on various websites. We used: <https://brucrafter.com/convert-brix-to-sg/>

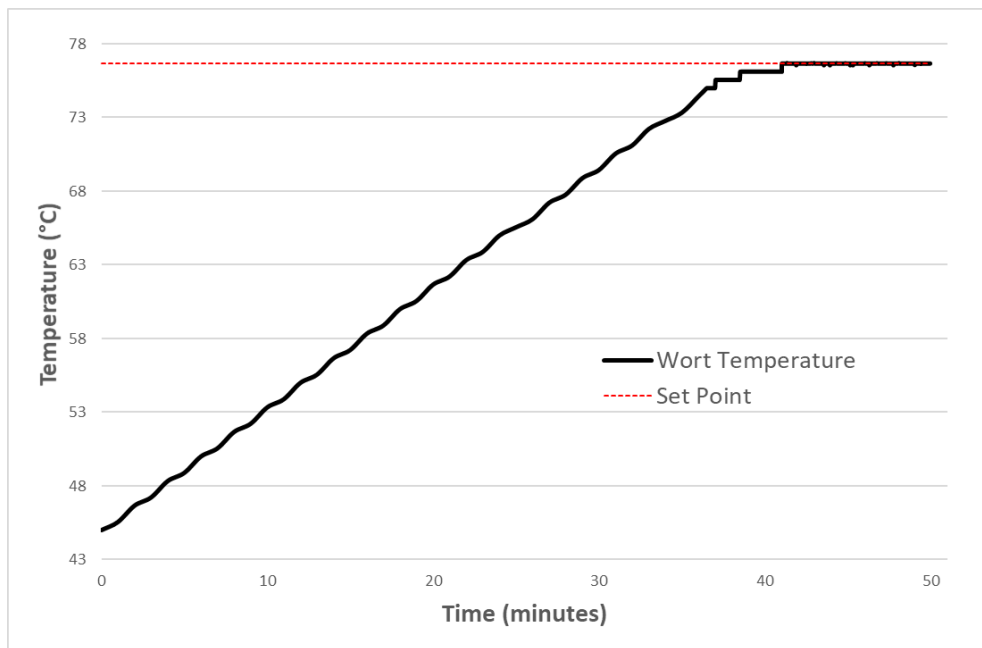
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## 9 **CONTROLS DATA ANALYSIS**

10

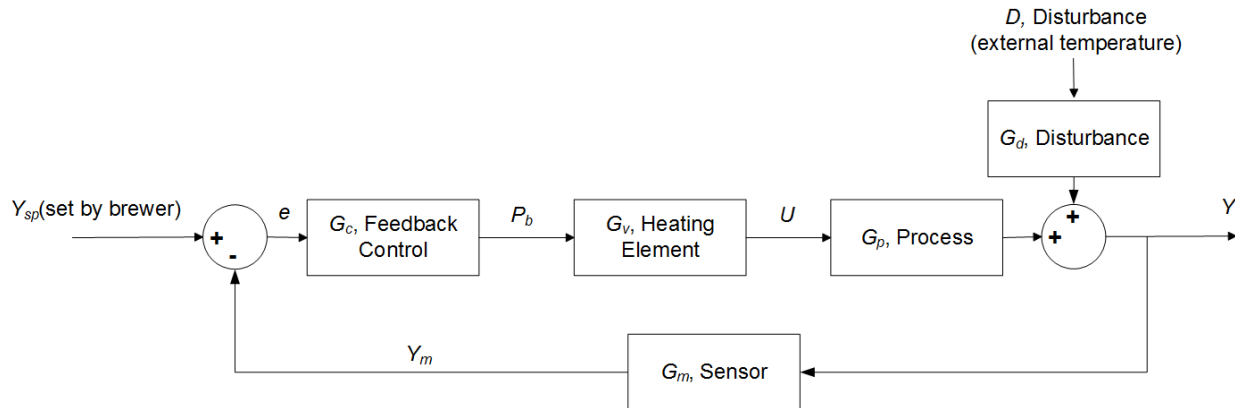
11 Students observe the advantage of process control in the brewing process, which is  
12 incorporated into many facets of engineering, and is directly applicable to Introduction to  
13 Automatic Process Controls course. Seemingly abstract material taught in the classroom is  
14 reinforced in a fun and interesting manner. Observing a system that uses process control for  
15 safety and product specifications physically demonstrates the importance of accurate system  
16 modeling, controller design, tuning, and sensor and valve selection, while highlighting the  
17 balance between performance and robustness.

1 In brewing, the temperature is the most important controlled variable (CV) because it  
2 ultimately affects taste and alcohol content. Through their brewing, students first briefly witness  
3 the system with no control. PID control is then used to demonstrate the ability of the engineer to  
4 control product quality with automated CV manipulation.<sup>[9]</sup>



5  
6 **Figure 5** Temperature control of the wort tank using PID. Strict adherence to the set point with  
7 no oscillation is a great demonstration of the benefits of derivative control  
8

9 One of the many advantages of a PID controlled process shown in Figure 5 is the ability  
10 to demonstrate the effects of changing controller parameters. This can be done in the controller,  
11 but it is easier, less expensive, and just as effective to do on a simulation of the actual process.  
12 Once students successfully model either the wort tank or the fermenter, control algorithms are  
13 applied to the modeled process.<sup>[9]</sup>



1  
2 **Figure 6** Block diagram for the temperature control law associated with the wort tank.  
3 Specifically,  $Y_{sp}$  is the temperature set point;  $e$  is the difference between the set point and the  
4 actual temperature,  $Y_m$ ; and  $P_b$  is the electricity sent to the heating element (if required) to  
5 produce the heat,  $U$ , required to change the temperature of the wort (the process). All of the  
6 “G” terms represent the transfer functions of the individual control loop elements.

7  
8 A tremendous learning opportunity is presented for cadets in the applying of various  
9 control laws (P, PI, PID) on the same process, while also demonstrating the importance of  
10 accurate tuning and establishing key parameters, such as gain and time constants. Cadets’  
11 classroom instruction is further reinforced when they see the process components physically  
12 during the construction of control block diagrams for the brewing process, like the one in Figure  
13 6. Block diagrams are a struggle for many students and pairing their physical observations with  
14 the diagrams is a valuable tool.

15 Exploring and describing the consequences of poor (or no) control on a process’s quality  
16 is a watershed in students’ understanding of process engineering. The ability to provide smooth  
17 and rapid responses to system changes is just as important as being flexible enough to handle a  
18 broad range of conditions and disturbances. Exploiting student-generated models in  
19 computational software allows educators to demonstrate and adequately discuss these important  
20 tradeoffs. After comparison of process data with modeled data, students gain appreciation for  
21 the importance of accurate modeling prior to control law implementation.<sup>[9]</sup>

1 A basic “PID control model” can be constructed to replicate the action of the wort  
2 heating element, where the cadets can use the following equations to analyze the model of  $u(t)$   
3 and  $e(t)$ , the controller effort and error signal, and incorporate an energy balance:

$$4 \quad u(t) = K_p \left( e(t) + \frac{1}{\tau_I} \int_0^t e(t) dt + \frac{1}{\tau_D} \frac{de(t)}{dt} \right), \quad (11)$$

$$5 \quad e(t) = T(t) - T_{set}, \quad (12)$$

6 where  $K_p$  is the gain,  $\tau_I$  is the integral constant and  $\tau_D$  is the derivative constant. Students, and  
7 arguably some operators in industry, typically are challenged by calculating and implementing  
8 tuning parameters in controllers. Having the ability to adjust tuning parameters using widely  
9 accepted methods provides the perfect environment for students to “see” the adjustments take  
10 effect. The energy balance for the on/off temperature controller is shown below:

$$11 \quad V_{tank} \rho_{wort} C_{p_{wort}} \frac{dT}{dt} = \dot{Q} \quad (13)$$

12 where  $\rho_{wort}$  is the density of the wort,  $C_{p_{wort}}$  is the heat capacity of the wort,  $V_{tank}$  is the tank  
13 volume, the quantity  $dT/dt$  is the time derivative of the temperature and  $\dot{Q}$  is the heat flow rate of  
14 the heater. With Eqs. 11-13, the cadets can design a basic controller and adjust the control  
15 parameters  $K_p$ ,  $\tau_I$ , and  $\tau_D$  until the control effort reaches zero with minimal oscillation, overshoot,  
16 or offset. In addition, the cadets can verify the appropriate heat was applied by analysis of the  
17 energy balance equation.<sup>[19]</sup>

## 18 HEAT AND MASS TRANSFER DATA ANALYSIS

19 The cooling of the boiled wort to an appropriate temperature for fermentation provides  
20 data for cadets to conduct both energy balances and heat exchanger design calculations.

1 Measuring the inlet and outlet temperatures of both the wort and the cooling water, as well as the  
2 volumetric flow rates, allows cadets to conduct an energy balance around the heat exchanger.  
3 Cadets gain experience in measuring quantities that, for the most part, have been abstract  
4 ‘givens’ in their academic careers. This provides great opportunities for demonstrating  
5 everything from a known-volume (sanitized) bucket and stop watch to more accurate rotameters.  
6 Discussions and calculations with uncertainties and error propagation necessarily follow as well.  
7 These calculations are directly applicable to the classroom or the lab in our Heat and Mass  
8 Transfer course, CH485. In addition, the cadets conduct similar analysis in the Chemical  
9 Engineering Lab course, CH459, using a single effect evaporator, also performing mass and  
10 energy balances and calculating the heat transfer coefficient.

11 After completing an energy balance, cadets use the data they have collected to analyze the  
12 plate heat exchanger used by the brewing crew. The wort is run in a single continuous flow through  
13 the plate heat exchanger, counter-current to the coolant water from a bench sink in the brewing  
14 room. From the flows and temperatures, they are required to calculate the overall heat transfer  
15 coefficient,  $Ua$ , for the heat exchanger, using Eqs. 14 and 15.

16 
$$Q_{load} = Ua\Delta T_{LM} , \quad (14)$$

17 where  $\Delta T_{LM}$  is the log mean temperature difference for countercurrent flow, defined as

18 
$$\Delta T_{LM} = \frac{(T_{cool\_Feed} - T_{wort\_exit}) - (T_{cool\_exit} - T_{wort\_Feed})}{\ln \left[ \frac{T_{cool\_Feed} - T_{wort\_exit}}{T_{cool\_exit} - T_{wort\_Feed}} \right]} . \quad (15)$$

19 where we define the parameters as follows:

20  $T_{cool\_Feed}$  is the coolant (utility) fluid feed temperature

21  $T_{cool\_exit}$  is the temperature of the coolant at the exit of the heat exchanger

1  $T_{wort\_Feed}$  is the feed temperature of the wort (process fluid)

2  $T_{wort\_exit}$  is the temperature of the wort at the exit of the heat exchanger.

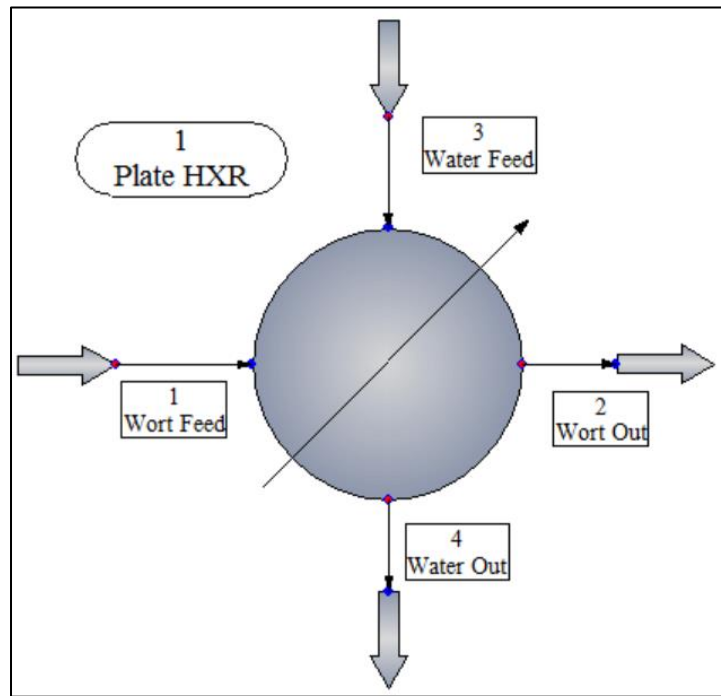
3 
$$Q_{load} = \dot{m}\hat{C}_{p\_wort}\Delta T_{wort} \quad (16)$$

4 where  $Q_{load}$  is the heat load for the heat exchanger,  $\dot{m}$  is the mass flow rate of the wort,  $\hat{C}_{p\_wort}$  is  
5 the average specific heat capacity of the wort, and  $\Delta T_{wort}$  is the change in temperature of the wort  
6 as it passes through the heat exchanger.

7         Because the cooling fluid is simply tap water from the bench sink, there is no control over  
8 the inlet temperature and only nominal control over the coolant flow rate. However, the wort flow  
9 can be varied using a pump, taking between 2 and 10 minutes to circulate a single fermenter of  
10 about 15 gallons. The equipment available did not allow immediate temperature feedback to  
11 demonstrate the initial time dependency of both the wort feed (slowly cooling from initial boiling)  
12 and exit temperatures. Though providing potential for future data, discussion, and modeling, the  
13 flow rates were assumed to be sufficient to allow the heat exchanger to reach steady state, making  
14 equations appropriate for modeling.

15         The lack of control of the cooling water flow rates and temperatures results in the data  
16 taken from every batch being different, with the most noticeable contrast between summer and  
17 winter brews where the inlet temperature can vary by several degrees. The varying data allows  
18 cadets, over time, to develop an accurate picture of how the heat transfer coefficient varies (or  
19 remains constant) as the conditions change. This variation is a great demonstration of why  
20 tabulated heat exchange coefficients<sup>[8]</sup> are general estimates, at best, and confirmation through  
21 experimental data is almost always required. Finally, cadets are able to model the heat exchanger  
22 within the CHEMCAD modeling software. They are able to develop their skills with the

1 simulation via several mechanisms. Wort is not one of the materials routinely found in the data  
2 library of the code, so cadets either have to choose a simulated fluid (water is usually a starting  
3 point for novice users), calculate a representative sugar content, or define their own material. They  
4 are able to compare their energy balance with that calculated from the actual flow data they take.<sup>[8]</sup>  
5 Figure 7 shows a CHEMCAD heat exchanger flowchart, while Figures 8 and 9 show the stream  
6 and equipment boxes from the CHEMCAD solution, which is in close agreement with our data  
7 from the analysis of the wort heat exchanger.



8  
9 **Figure 7** Screen shot of the input display of a simple, two-inlet, heat exchanger in CHEMCAD.  
10 The simulation can be configured for frame-and-plate heat exchangers, exploring heat transfer  
11 coefficients and areas, fouling factors, flow rates, and materials, including wort characteristics.  
12

1  
2 **Table 5.** An example CHEMCAD stream report showing the properties of the flow streams from  
3 Figure 7. The data can be used in energy balance calculations and compared to measured values.

Stream No	1	2	3	4
Name	Wort Feed	Wort Out	Water feed	Water Out
--Overall--				
Temp C	99.9000	20.0000	15.5600	57.4324
Enth MJ/sec	-1.3011	-1.3291	-2.5437	-2.5157
Mass flow kg/s	0.0837	0.0837	0.1600	0.1600
Std liq cc/sec	83.7001	83.7011	160.0002	160.0002
--Liquid only--				
Mass flow kg/s	0.0837	0.0837	0.1600	0.1600

4  
5 **Table 6.** A sample equipment table from CHEMCAD showing the heat exchange coefficient,  $U$ ,  
6 and heat exchanger area,  $a$ , calculated by the simulation for the properties specified.

<b>Equip. No.</b>	<b>1</b>
<b>Name</b>	<b>Plate HXR</b>
<b>1<sup>st</sup> Stream T Out C</b>	<b>20.0000</b>
<b>Shells in Series</b>	<b>1</b>
<b>No. of SS Passes</b>	<b>1</b>
<b>No. of TS Passes</b>	<b>1</b>
<b>Calc Ht Duty MJ/sec</b>	<b>0.0280</b>
<b>LMTD (End Points) C</b>	<b>16.8406</b>
<b>LMTD Corr Factor</b>	<b>1.0000</b>
<b>Calc U W/m<sup>2</sup>-K</b>	<b>1849.1259</b>
<b>Calc Area m<sup>2</sup></b>	<b>0.9000</b>

7  
8 Modifying equations 14 and 16, as shown below, we calculate the product  $Ua$

9 
$$(\rho C_p \Delta T \dot{V})_{\text{cooling water}} = (\rho C_p \Delta T \dot{V})_{\text{wort}} \quad (17)$$

10 
$$(\rho C_p \Delta T \dot{V})_{\text{cooling water}} = UA \Delta T_{\text{lm}} \quad (18)$$

11 where  $\rho$  is the density of the water and wort respectively (1.0 and 1.06 g/mL);  $C_p$  is the heat  
12 capacity assumed to be the same for both water and wort;  $\Delta T$  is the temperature difference between  
13 the inlet and outlet, and  $\dot{V}$  is the volumetric flow rate,  $U$  is the overall heat transfer coefficient,  $a$   
14 is the surface area, and  $\Delta T_{LM}$  is the log mean temperature difference for countercurrent flow.



1 For a verification of the CHEMCAD simulation, we turn to the Therminator Performance  
2 Data shown in the Therminator Owners Manual.<sup>[20]</sup> The performance data figure of the manual  
3 uses the following parameters: wort specific gravity of 1.04; wort outlet temperature of 68°F  
4 (20°C), and wort inlet temperature of 212°F (100°C). Choosing a cooling water inlet temperature  
5 of 60°F (15.6°C) and cooling water flow rate of 2.5 gallons per minute, the required wort flow rate  
6 is approximately 1.25 gallons per minute. These are the values (with converted units) used in the  
7 simulation demonstrated in Figures 7 to 9. Although a value of  $Ua$  is not available from the  
8 owner's manual, the charted flow values match very nearly to those calculated by CHEMCAD. In  
9 the future, careful measurement of inlet and outlet temperatures will allow more direct calculation  
10 of  $Ua$  and comparisons to the manufacturer's performance data.

## 11 **PROCESS ECONOMICS AND PRODUCT ENGINEERING**

12 Data for analysis of the profitability (or lack thereof) of our brewing process is shown in  
13 Tables 7 to 9 to 7.

**Table 7:** *Pints & (\$) of Kicking Mule Produce per batch calculation*

Volume	Gallons	Pints	Cost (\$)/pint	Total (\$)/ batch
	16	128	2.50	320.00

14

15

1

**Table 8: Cost Analysis per Batch**

<b>Batch Cost</b>	
<b>Ingredient</b>	<b>Cost (\$)</b>
Yeast	20.00
Hops	20.00
Bulk Grain and Additives	20.00-40.00
CO2	-
Total Spent (\$)	80.00
Total Brought in (\$)	320.00
Profit (\$) per Batch	240.00

2

3           Based on a careful analysis of the data shown in Table 7, we can produce a maximum of  
4 16 gallons of Kicking Mule per batch, correlating to 128 pints. At \$2.50/pint, the going rate of a  
5 pint of Kicking Mule, we earn \$320.00 per batch of Kicking Mule. By subtracting off the cost of  
6 a batch of Kicking Mule: \$20.00 for yeast; \$40.00 for grain and additives; and \$20.00 for hops our  
7 profit per batch is roughly \$240.00.

**Table 9: Long Term Investment Cost**

<b>Long Term Investment</b>	
<b>Equipment</b>	<b>Cost (\$)</b>
Heat Exchanger	200.00
Refrigerator	150.00
Grinder	100.00
Batch Reactor	1000.00
EHERMs	4700.00
Total:	6150.00

1           Considering the overall investment in the equipment necessary for the operation (described  
2 in Figure 2), we see the total initial cost is \$6150.00. With a profit per batch of \$280.00 it will  
3 take approximately 26 batches of kicking mule to recoup the cost of the initial investment.

4           As an extracurricular activity, some standard economic expenses are not evaluated in this  
5 process. Most notably, labor costs, traditionally a significant portion of operational costs, are not  
6 included in this basic analysis. Other considerations, including estimated values of depreciation,  
7 equipment replacement or maintenance timelines and costs, utility costs, and even interest rates  
8 can be used for more complex and long-term analyses of the sustainability of the process. When  
9 viewed as a pilot plant, these more detailed economic concerns can be analyzed within the  
10 context of scaling this batch system to a more industrial scale where such considerations are  
11 critical and cannot be assumed as negligible.

12           With respect to quality control, each recipe is diligently recorded, and notes taken about  
13 the quality of the flavor, coloring, alcohol content etc. for future Kicking Mule batch  
14 reproduction. Typically, the overall batch quality is determined qualitatively and quantitatively  
15 through measurements of density (then converted to alcohol content), coloring and informal  
16 surveys from the point of sale.

## 17 **CONCLUSION**

18           Fundamentally, the beer brewing operations of the Kicking Mule Brewing Co. allow the  
19 members of the club to put into practice the chemical engineering principles they have learned  
20 (or will learn) through their classroom and laboratory experiences. Their learning is enhanced  
21 through real-world measurements, data analysis, uncertainty propagation, and, ultimately, the  
22 production of a useable, saleable, product that meets the needs (wants) of a client. In the future,

1 there is the potential for even more exploration of various chemical engineering principles,  
2 including jacket heat exchangers, batch chemical reactors, the economic and profitability  
3 analysis, etc. It should also be noted that the data generated in the execution of a single batch of  
4 Kicking Mule can be used in the context of the reactor design, controls and heat transfer  
5 chemical engineering electives. The focus has been, and will continue to be, providing an  
6 excellent, but continually improving, undergraduate chemical engineering education.

7

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12 Military Academy, the Department of the Army, or the Department of Defense.

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10 **Author Bios**



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